# Free Energy Relationship for Electron Transfer Far from Equilibrium. Analysis of Reversibility in the Endergonic Region

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Abstract: Electron-transfer rate constants are measured over an extended range of the free energy change ( $\Delta G$ ) for a single system. Since the experimental free energy relationship encompasses both the exergonic and endergonic extremes, it dramatically emphasizes the existence of curvature that previously had been observed only over a much narrower span of  $\Delta G$ . The kinetic measurements employ a cyclic voltammetric technique that allows the free energy change for electron transfer to be continuously tuned to the applied electrode potential E. The resulting free energy relationship for outer-sphere electron transfer from the organometal Me<sub>2</sub>Co(DpnH) exhibits a limiting behavior of the experimental transfer coefficient ( $\beta_e$ ), which approaches 0 in the exergonic limit and 1 in the endergonic limit, as shown in Figure 3. Kinetic and error analyses of the electrochemical technique demonstrate that in the exergonic region [i.e., as one proceeds beyond  $E^{\circ} = 0.53$  V for Me<sub>2</sub>Co(DpnH)], the experimental rate constant  $k_e$  represents an accurate representation of the *intrinsic* rate constant  $k_1$  for electron transfer. However, as one drops into the endergonic region below 0.53 V, the reversibility in the electron-transfer step becomes increasingly more important, and  $k_e$  can only be explicitly related to  $k_1$  by specifically taking into account the decomposition rate constant  $k_2$  of the organometal cation. The general kinetic solution given in eq 10 then allows the intrinsic rate constant  $k_1$  to be determined in the endergonic region. It is noteworthy that the excellent fit of the resulting rate data to the Rehm-Weller free energy relationship can be achieved with a single value of the intrinsic barrier  $\Delta G_0^*$  over the entire span of the free energy change. The evaluation of the standard reduction potentials for irreversible systems is described in the context of the Marcus theory for outer-sphere electron transfer.

The Marcus theory of electron transfer has provided a quantitative means of analysis of outer-sphere mechanisms.<sup>1-3</sup> It is particularly useful for predicting electron-transfer rates near the equilibrium potential, such as the self-exchange processes. However, its applicability decreases as the free energy change is removed from this benchmark. Although several empirical free energy relationships are known,  $^{4-7}$  no adequate theory exists for the description of the energy gamut that simultaneously includes the exergonic as well as the endergonic limits.8-11

The desirability of an extended free energy relationship stems from its importance to systems that undergo interesting chemistry attendant upon electron transfer. These include an ever increasing number and variety of organic and organometallic systems in

which questions relating to the involvement of (single) electron transfer or "SET" mechanisms have arisen.<sup>12</sup> For these chemically irreversible systems, electron-transfer rates are often measureable only at potentials far removed from equilibrium.<sup>13,14</sup>

A basic experimental challenge is thus to establish the functional dependence of the rate of electron transfer over an extended region of the free energy change ( $\Delta G$ ). Most of the electron-transfer studies have heretofore been carried out in homogeneous systems in which the chemical oxidants and reductants are both in solution.<sup>15</sup> Such homogeneous studies are circumscribed by the availability of chemical oxidants and reductants with standard reduction potentials sufficient to span only a limited range of  $\Delta G^{*}$ Furthermore, varying structures with different steric properties as well as changing magnitudes of the reorganization energies must be employed to encompass an extended span. Thus there are advantages to be gained in the study of a single system over a wide range of  $\Delta G$ . Electrochemical oxidation and reduction provide such an opportunity, and it is somewhat surprising that only a limited number of systems have been examined with this end in mind. In particular, the electrochemical EC mechanism outlined in the simple kinetic Scheme I is an especially viable one for covering wide ranges in the free energy change. For example,

<sup>(1)</sup> Marcus, R. A. J. Phys. Chem. 1963, 67, 853

<sup>(2)</sup> Marcus, R. A. Annu. Rev. Phys. Chem. 1964, 15, 155.

<sup>(3)</sup> Marcus, R. A. In "Tunneling in Biological Systems"; Chance, B., et al., Eds.; Academic Press: New York, 1979; p 109 ff.

<sup>(4)</sup> Rehm, D.; Weller, A. Ber. Bunsenges. Phys. Chem. 1969, 73, 834. Isr. J. Chem. 1970, 8, 259.

<sup>(5)</sup> Marcus, R. A. J. Phys. Chem. 1968, 72, 891.

<sup>(6)</sup> Evans, M. D.; Polanyi, M. Trans. Faraday Soc. 1936, 32, 1340. 1938, 34, 11.

<sup>(7) (</sup>a) For a current assessment of free energy relationships in electron transfer, see: Scandola, F.; Balzani, V.; Schuster, G. B. J. Am. Chem. Soc. 1981, 103, 2519. (b) Free energy relationships, also referred to as rateequilibrium relationships and structure-reactivity correlations, have also been quantitatively treated for other types of reactions in a more general context. For summaries, see: (c) Murdoch, J. R. Ibid. 1972, 94, 4410. (d) Agmon, N. Int. J. Chem. Kinet. 1981, 13, 333.

<sup>(8)</sup> The lack of a theoretical model arises, at least in part, from the scarcity of reliable experimental data for systems far removed from the equilibrium potential. Indeed the concentration of the electron-transfer literature for systems at or close to the equilibrium potential is often dictated by experimental considerations. Thus the measurements of electron-transfer rates of substitution-stable oxidants and reductants are most conveniently carried out at the equilibrium potentials, both in homogeneous chemical and heterogeneous electrode processes.  $^{9\!-\!11}$ 

<sup>(9) (</sup>a) Reynolds, W. L.; Lumry, R. W. "Mechanisms of Electron Transfer"; Ronald Press: New York, 1966. (b) Delahay, P. "The Electric Double Layer and Electrode Kinetics"; Interscience: New York, 1965. (10) (a) Reinmuth, W. H. Anal. Chem. 1964, 36, 211R. (b) Vetter, K.

<sup>(1) (</sup>a) Reinhuti, w. H. Anda. Chem. 1966, 56, 211K. (b) Vettel, R. J. "Electrochemical Kinetics"; Academic Press: New York, 1967.
(11) (a) Pletcher, D. Chem. Soc. Rev. 1975, 75, 1190. (b) Streitwieser, A. In "Physical Methods in Chemistry"; Weissberger, A., Rossiter, B. W., Eds.; Wiley: New York, 1971; Part IIa. (c) Schmidt, P. P. Electrochemistry 1975, 5, 21. 1976, 6, 128.

<sup>(12) (</sup>a) The vogue among some is to refer to organic and organometallic mechanisms that proceed via electron transfer as single electron transfer or SET. (b) For examples of electron transfer in such processes, see: Kochi, J. K. "Organometallic Mechanisms and Catalysis"; Academic Press: New York, 1978. Ashby, E. C.; Goel, A. B.; DePriest, R. N.; Prasad, H. S. J. Am. Chem. Soc. 1981, 103, 973, and related papers. Bordwell, F. G.; Clemens, A. H. J. Org. Chem. 1981, 46, 1035. Chanon, M. Angew. Chem. 1982, 21, 1. A wide variety of photochemical processes involving electron transfer in the quenching of excited states is also known. For some leading references, see: Geofroy, G. L.; Wrighton, M. S. "Organometallic Photochemistry"; Academic Press New York, 1979. Adamson, A. W.; Fleischauer, P. D., Eds; "Concepts of Inorganic Photochemistry"; Wiley: New York, 1975.

<sup>(13)</sup> For systems in which reduction potentials are known, see: (a) Andrieux, C. P.; Blocman, C.; Dumas-Bouchiatt, J. M.; Saveant, J. M. J. Am. Chem. Soc. 1979, 101, 3431. (b) Klingler, R. J.; Kochi, J. K. Ibid. 1980, 102, 4790.

<sup>(14)</sup> For systems in which reduction potentials are not established, see: (a) Schuster, G. B. J. Am. Chem. Soc. 1979, 101, 5851 and references therein. Scandola, F.; Balzani, V.; Schuster, G. B. Ibid. 1981, 103, 2519. (b) For the kinetic ambiguity, see: Walling, C. Ibid. 1980, 102, 6854. (15) Cannon, R. D. "Electron-Transfer Reactions"; Butterworths: Boston, 1000.

<sup>1980.</sup> 

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Scheme I

$$\mathbf{A} \underbrace{\frac{k_1}{k_4}}_{k_4} \mathbf{A}^+ + \mathbf{e} \tag{1}$$

$$A^+ \xrightarrow{k_2} \text{product}$$
 (2)

the rate of the forward electron transfer in eq 1 is readily and continuously tuned by the applied electrode potential over a wide range, the relationship simply being<sup>16</sup>

$$k(E) = k_{\rm s} \exp\left[\frac{\beta n \mathcal{F}}{RT} (E - E^{\circ})\right]$$
(3)

where E is the electrode potential, n is the number of electrons transferred from the electroactive species A in the rate-limiting step,  $\beta$  is the transfer coefficient for the electrode process, and  $E^{\circ}$  is the standard reduction potential, which fixes the value of  $k_s$ , the standard rate constant.  $\mathcal{F}$  is the Faraday constant, and R and T have their usual significance. Although Scheme I illustrates the kinetics of the oxidation of the electroactive species A, the same basic notion applies, of course, to its reduction. The use of transient electrochemical techniques such as the readily available cyclic voltammetry allows the rate of the followup process to be varied simply by altering the sweep rate.<sup>17</sup> Thus the degree of reversibility in eq 1 is an experimental variable that can be examined over a wide range of electron-transfer rates.

In previous studies we have shown how organometals are ideally suited to be utilized as electron donors in electrochemical EC systems.<sup>18</sup> Among the various organometals examined, the organocobalt macrocycle typified by Me<sub>2</sub>Co(DpnH)<sup>19,20</sup>



is unusually well-suited in that the essential kinetic features of Scheme I have all been verified. Thus, the first-order decay of the radical cation  $A^+ = Me_2Co(DpnH)^+$  proceeds with the rate constant  $k_2 = 10^5 \text{ s}^{-1}$ . The zero-order dependence on the unoxidized species  $A = Me_2Co(DpnH)$  has been demonstrated, and the distinction between a one- and two-electron electrode process has been established by competition kinetics with suitable trapping methods.<sup>19</sup> In addition, the direct comparison with electron transfer effected by various chemical oxidants in solution has delineated the fundamental unity of outer-sphere electron transfer between heterogeneous electrochemical and homogeneous chemical processes in these systems.<sup>13b</sup> This large body of mechanistic information is unusually valuable since it now provides us with the necessary support to focus on the measurement of the rates of electron transfer over an extended range of the free energy change, i.e., the applied electrode potential  $E^{21}$  We wish to show how the resulting potential dependence of the rate bears critically



Figure 1. Single-scan cyclic voltammogram of  $3.3 \times 10^{-3}$  M Me<sub>2</sub>Co-(DpnH) in acetonitrile solutions containing 0.1 M TEAP at various scan rates. Electrode potentials in volts vs. saturated NaCl SCE.

on the free energy relationships for electron transfer, especially as they are affected by the reversibility in Scheme I. The evaluation of the transfer coefficient  $\beta$  forms an important basis of this analysis.<sup>22</sup>

## Results

The experimental determination of the electron-transfer rates derives from the cyclic voltammetric technique described in detail for Me<sub>2</sub>Co(DpnH). The free energy correlation of the experimental rate constant  $k_e$  is then established over an extended range of the free energy change for this system.

Cyclic Voltammetry of Me<sub>2</sub>Co(DpnH). The cyclic voltammograms (CV) of Me<sub>2</sub>Co(DpnH) were recorded at 25 °C with a stationary platinum microelectrode in acetonitrile solutions containing 0.1 M tetraethylammonium perchlorate (TEAP). The initial positive scan cyclic voltammogram illustrated in Figure 1 is characterized by an anodic wave showing a well-defined current maximum but no coupled cathodic wave on the reverse scan, even at sweep rates up to  $10^3$  V s<sup>-1</sup> and at temperatures as low as -80 °C. A closer inspection of the details of the sweep dependence reveals that the current in the initial portion (i.e., foot) of the CV wave is singularly independent of the sweep rate. The foot of an electrochemical wave represents an important limiting situation in which the concentration of the electroactive species is effectively constant and equal to that in the bulk solution. Thus the current in the earliest portion of the CV wave may be analyzed solely on the basis of the electron-transfer process, without reference to diffusion of the reactants to the electrode.<sup>23</sup> Indeed the lack of dependence of the current on the sweep rate for a considerable portion of the foot (see Figure 1) confirms the net forward rate of electron transfer from Me<sub>2</sub>Co(DpnH) to be independent of the diffusion of the products away from the electrode surface. (Note that the rate of diffusion is known to be proportional to the square root of the sweep rate.<sup>24</sup>) Kinetically such a situation would arise in Scheme II if the decomposition of the oxidized Me<sub>2</sub>Co(DpnH) in eq 5 were more facile than the reverse rate of electron transfer in eq 4, where M = DpnH.<sup>19,20</sup> Inspection of the CV curves in ~ .

$$Me_2CoM \stackrel{k_1}{\underset{k_1}{\longleftarrow}} Me_2CoM^+ + e$$
 (4)

$$Me_2CoM^+ \xrightarrow{k_2} Me_{\cdot} + MeCoM^+$$
, etc. (5)

Figure 1 also reveals a peak broadening that accompanies the increasing sweep rates. The nature of this apparent change in electrochemical reversibility is described in detail in the Experimental Section.

<sup>(16)</sup> Bauer, H. H. J. Electroanal. Chem. Interfacial Electrochem. 1968, 16, 419.

<sup>(17)</sup> The followup process consists of the sum of the homogeneous rate constant  $k_2$  for the decomposition of  $A^+$  and the diffusion of  $A^+$  from the electrode surface. Altering the sweep rate changes the diffusion rate. See: Galus, Z. "Fundamentals of Electrochemical Analysis"; Wiley: New York, 1976.

<sup>(18)</sup> Klinger, R. J.; Kochi, J. K. J. Phys. Chem. 1981, 85, 1731, and ref 13b.

<sup>(19)</sup> Tamblyn, W. H.; Klingler, R. J.; Hwang, W. S.; Kochi, J. K. J. Am. Chem. Soc. 1981, 103, 3161.

<sup>(20)</sup> DpnH = 2,3,9,10-tetramethyl-1,4,8,11-tetraazaundeca-1,3,8,10-tetracen-11-ol-1-olate.

<sup>(21)</sup> For electron-transfer processes, note that the variation in the applied potential E at an electrode is equivalent to using a graded series of oxidants (or reductants) with different standard potentials  $E^{\circ}$  in a homogeneous chemical process. The driving force or free energy change is then given by  $\Delta G = -n\mathcal{F}(E - E^{\circ})$ .

<sup>(22)</sup> In electrochemical kinetics, the dependence of the rate constant on the driving force is usually referred to as the *transfer* coefficient  $\beta$ , which in homogeneous chemical kinetics is generally designated as the *Brønsted* coefficient  $\alpha$ .

<sup>(23)</sup> Reinmuth, W. H. Anal. Chem. 1960, 32, 1891.

<sup>(24)</sup> Adams, R. W. "Electrochemistry at Solid Electrodes"; Dekker: New York, 1969.



Figure 2. The constancy of the experimental rate constant  $k_e$  for electron transfer with the variation in the CV sweep rate at E = 0.578, 0.488, 0.428, and 0.368 V vs. saturated NaCl SCE.

To evaluate the kinetic situation in Scheme II quantitatively we now make a rigorous conversion of the current-potential profiles in Figure 1 to the rate constant  $k_e$  for the *net forward* electron transfer at the various electrode potentials, i.e., the free energy changes.

Evaluation of the Heterogeneous Rate Constants for Electron Transfer from the Cyclic Voltammogram. The heterogeneous rate constant for the net forward electron transfer is proportional to the electrochemical current. At a given applied potential E, the rate constant  $k_e$  is related to the current i(E) by the expression<sup>25</sup>

$$k_{\rm e}(E) = i(E) / [n \mathcal{F} A C(t)] \tag{6}$$

where A is the area of the electrode and C(t) is the time-dependent concentration of the electroactive species (i.e., Me<sub>2</sub>Co(DpnH)) at the electrode surface. The values of C(t) can be evaluated from the current-time history by using the convolution integral<sup>26</sup>

$$C(t) = C^{0} \left[ 1 - \frac{10^{3}}{n \mathcal{F} A C^{0} (\pi D)^{1/2}} \int_{0}^{t} \frac{i(\eta)}{(t-\eta)^{1/2}} \, \mathrm{d}\eta \right]$$
(7)

where  $C^{\circ}$  is the initial concentration of Me<sub>2</sub>Co(DpnH) in the bulk solution, as described in detail in the Experimental Section. It is important to emphasize that eq 7 is kinetically rigorous since it derives directly from Fick's laws of diffusion.<sup>27</sup> The validity of eq 7 is independent of the nature or complexity of the kinetic scheme provided the only means of depleting (or of increasing) the total amount of electroactive species involves the transfer of charge—in other words, the current i(E) must be faradaic. It pertains to cases such as that in Scheme II in which the electroactive species are thermally stable and are not catalytically regenerated via a nonfaradaic pathway from the products of electrolysis.<sup>19</sup> The use of eq 6 and 7 thus allows values of the rate constants  $k_e$  for heterogeneous electron transfer to be evaluated from the current-potential data contained in the cyclic voltammogram. In practice, the faradaic current is obtained from the observed current after correction for the charging current. Since the charging current increases linearly with the sweep rate, in contrast to a square-root dependence of the faradaic current with sweep rate, the error in the measurement of the faradaic current increases with the sweep rate. As a result, the observed current as well as the charging current must be measured precisely under the same conditions, particularly at high sweep rates. A detailed description of the experimental procedure is given separately in the Experimental Section. Table I summarizes typical values of the experimental rate constant  $k_e$  obtained at various applied potentials E. A more extended list of  $k_e$  and E, including all the data employed in this study, is tabulated in the supplementary material.

Table I. Heterogeneous Rate Constants for Electron Transfer from  $Me_2CO(DpnH)$  by Convolutive Potential Sweep Voltammetry<sup>a</sup>

v, <sup>b</sup> V s <sup>-1</sup>	<i>i</i> ( <i>E</i> ), mA	<i>i</i> <sub>c</sub> , mA <sup>c</sup>	$E, V^d$	$\frac{\log k_{\rm e}}{\rm cm \ s^{-1}}$	$\log k_1, \\ \operatorname{cm s}^{-1}$
0.03	0.0092	0.0004	0.318	-3.6800	-3.1969
0.03	0.0212	0.0004	0.347	-3.2700	-2.9171
0.03	0.0406	0.0004	0.373	-2.8900	-2.6028
0.03	0.0603	0.0004	0.399	-2.5600	-2.3559
0.03	0.0688	0.0004	0.421	-2.3000	-2.1518
0.06	0.0287	0.0007	0.356	-3.0600	-2.6223
0.06	0.0914	0.0007	0.416	-2.1800	-1.9097
0.10	0.0412	0.0026	0.368	-2.9300	-2.5962
0.10	0.0936	0.0028	0.406	-2.3900	-2.1519
0.30	0.0315	0.0079	0.346	-3.2100	-2.7361
0.30	0.0745	0.0096	0.383	-2.7200	-2.4323
0.30	0.1485	0.0086	0.414	-2.2700	-2.0430
0.30	0.2155	0.0107	0.446	-1.8800	-1.7333
0.60	0.0555	0.0079	0.361	-2.9100	-2.3283
0.60	0.2540	0.0095	0.437	-1.9700	-1.7954
1.00	0.0790	0.0152	0.377	-2.7900	-2.4703
1.00	0.1840	0.0169	0.416	-2.3000	-2.1120
1.00	0.3540	0.0181	0.460	-1.8000	-1.7033
3.00	0.0890	0.0244	0.368	-2.7800	-2.1647
3.00	0.2070	0.0144	0.409	-2.2600	-1.9534
3.00	0.3430	0.0178	0.435	-1.9800	-1.7931
3.00	0.6070	0.0261	0.4/6	-1.5200	-1.4211
3.00	0.6980	0.0283	0.301	-1.2500	-1.1830
10.00	0.2920	0.0504	0.412	-2.2000	-1.6636
10.00	0.3280	0.0366	0.441	-1.6300	-1.0470
10.00	1.06	0.0024	0.472	-1.3300	-1.4130 -1.2238
10.00	1.00	0.07	0.795	-1.0100	-0.9655
1000 00	3.40	3 30	0.525	-0.9500	-0.9144
1000.00	3.84	3 74	0.554	-14500	-1.4471
800.00	3.94	3 40	0.620	-0.6200	-0.6174
666.00	3.68	3.22	0.610	-0.4300	-0.4241
500.00	3.33	2.85	0.626	0.800	0.0902
300.00	1.58	1.30	0.514	-1.5400	-1.5204
225.00	2.25	1.16	0.588	-0.7200	-0.7129
225.00	1.65	1.01	0.540	-1.1000	-1.0804
175.00	1.41	0.83	0.530	-1.1200	-1.0921
175.00	2.27	0.88	0.596	-0.4500	-0.4403
175.00	2.20	0.86	0.590	-0.5100	-0.4993
143.00	2.11	0.73	0.608	-0.1900	-0.1789
143.00	2.10	0.72	0.596	-0.3200	-0.3068
114.00	0.7420	0.5002	0.468	-1.5300	-1.3922
114.00	1.77	0.60	0.586	-0.3500	-0.3317
114.00	1.67	0.54	0.566	-0.4400	-0.4071
89.00	0.8140	0.4422	0.492	-1.2600	-1.1639
89.00	0.7760	0.4377	0.482	-1.6200	-1.5605
89.00	1.38	0.48	0.542	-0.6700	-0.6195
89.00	1.21	0.44	0.524	-0.8200	-0.7459
67.00	0.5540	0.3784	0.472	-1.6900	-1.6138
67.00	1.20	0.44	0.554	-0.7900	-0.7668
67.00	0.4840	0.3656	0.458	-1.8600	-1.7696
67.00	0.7640	0.3936	0.502	-1.2900	-1.2318
67.00	1.18	0.43	0.548	-0.8000	-0.7711
67.00	0.5300	0.3564	0.464	-1.6800	-1.5693
67.00	1.19	0.41	0.540	-0.7800	-0.7380

<sup>a</sup> In acetonitrile solution containing 0.1 M tetraethylammonium perchlorate at 25 °C. <sup>b</sup> Sweep rate. <sup>c</sup> Charging current. <sup>d</sup> Applied potential vs. saturated NaCl SCE.

The results in Figure 2 demonstrate that the rate constants (log  $k_e$ ) obtained in this manner are indeed independent of the sweep rate (log v), varied over 4.2 orders of magnitude. The four values of the applied potential were arbitrarily chosen to cover the entire breadth of the CV waves in Figure 1. Note that the scatter in the data is more pronounced at the faster sweep rates, owing to the larger errors in the measurement of the faradaic current described above.

The rate constant at a particular potential was obtained by averaging the values obtained at various sweep rates, and it is plotted against the applied potential E in Figure 3. The smooth variation covers a span of  $2 \times 10^3$  in the rate constant and a span of more than 0.4 V in the free energy change for heterogeneous

<sup>(25)</sup> Delahay, P. "New Instrumental Methods in Electrochemistry"; Interscience: New York, 1954.

<sup>(26)</sup> Saveant, J. M.; Tessier, D. J. Phys. Chem. **1978**, 82, 1723. Note that eq 7 and 25 in ref 49 should be corrected to those given here. A factor of  $10^3$  has also been omitted in eq 7 of ref 27.

<sup>(27)</sup> Imbeaux, J. C.; Saveant, J. M. J. Electroanal. Chem. Interfacial Electrochem. 1973, 44, 169.



Potential, volts

Figure 3. The variation in the experimental rate constant  $k_e$  for electron transfer as a function of applied potential (free energy change). The limiting slope in the endergonic region is shown by the fit to the line arbitrarily drawn with a slope of unity. For a direct comparison of log  $k_e$  and the potential, a multiplicative factor of  $2.3RT/\mathcal{F}$  must be included.

electron transfer.<sup>28</sup> Two features are noteworthy in Figure 3. First, at the low-potential end, the limiting slope of the relationship between the activation free energy (log  $k_e$ ) and the applied potential (E) is close to unity, as shown by the line of unit slope included in Figure 3. Second, at the other limiting extreme, of high potential, the net forward rate constant for electron transfer is observed to be clearly leveling off and *becoming* independent of the applied potential. At this juncture it is important to emphasize that the intermediate slope of 0.5 occurs in Figure 3 as a tangent at only the *middle* (E = 0.53 V) of an obvious curve. Therefore from a strictly graphical or mechanical point of view, 0.5 cannot possibly represent a limiting value of the slope in this system. The variation of the experimental rate constant  $k_e$  for electron transfer is thus clearly nonlinear over the extended range of the free energy change in Figure 3.

### Discussion

The electron-transfer rate behavior so graphically illustrated in Figure 3 is unique, and we know of no other kinetic measurement in which both limiting kinetic extremes have been covered, particularly in a single system. Consequently, we now wish to exploit the experimental information contained in Figure 3 to develop the free energy relationship for electron transfer over an extended range. To determine the functional dependence of the rate constant for electron transfer with the free energy change, we must first clearly delineate the distinction between the ex*perimental* rate constant  $k_e$  and the *intrinsic* rate constant  $k_1$  for forward electron transfer in Scheme I. Indeed, the relationship between the two rate constants is critically dependent on the lifetime of the electrogenerated intermediate A<sup>+</sup>, which is determined from the magnitudes of the rate constant  $k_{-1}$  for back electron transfer and the rate constant  $k_2$  for decomposition, as graphically illustrated here.

$$A \xrightarrow{k_{e}} e + A^{+} \xrightarrow{k_{2}} product$$

The rigorous combination of the kinetics of Scheme I with Fick's laws of diffusion affords the relationship among these rate constants:

$$k_{\rm e} = k_1 [k_2' / (k_{-1} + k_2')] \tag{8}$$



Figure 4. Free energy relationship for the intrinsic electron-transfer rate constant  $k_1$  obtained from the experimental rate constant  $k_e$  after correction for reversibility according to eq 10. The line represents  $\beta = 1/2$ , and  $E^{\circ}$  is determined as described in the text. For a direct comparison of log  $k_e$  and the potential, a multiplicative factor of  $2.3RT/\mathcal{F}$  must be included.

which is the same as that obtained from a straightforward steady-state treatment.<sup>29</sup> (Note that the homogeneous rate constant  $k_2$  in Scheme I has been converted to its heterogeneous equivalent  $k_2'$  for use in eq 8.<sup>31</sup>)

**Evaluation of the Intrinsic Rate Constant**  $k_1$  for Electron Transfer. The evaluation of the intrinsic rate constant  $k_1$  proceeds from the rearrangement of eq 8:

$$k_{1} = k_{e}k_{2}' \left( k_{2}' - k_{e} \frac{k_{-1}}{k_{1}} \right)^{-1}$$
(9)

followed by the combination with the Nernst expression<sup>32</sup> to yield eq 10. The complete kinetic expression in eq 10 relates the

$$k_{1} = k_{e}k_{2}' \left\{ k_{2}' - k_{e} \exp\left[\frac{-n\mathcal{F}}{RT}(E - E^{\circ})\right] \right\}^{-1}$$
(10)

experimental rate constant  $k_e$  with the forward rate constant  $k_1$ for electron transfer as a direct function of the decomposition rate constant  $k_2'$  and the standard reduction potential  $E^0$ . Since an independent measurement of  $k_2' = 1.2 \text{ cm s}^{-1}$  or  $k_2 = 10^5 \text{ s}^{-1}$  is available for Me<sub>2</sub>Co(DpnH)<sup>+</sup> from the previous study,<sup>19</sup> it can be used in conjunction with  $E^\circ = 0.53 \text{ V}^{33}$  to convert the experimental  $k_e$  listed in Table I to the intrinsic rate constant  $k_1$ for forward electron transfer in Scheme I. The results of the kinetic analysis for the intrinsic rate constant  $k_1$  based on eq 10 are replotted in Figure 4.

(30) Nadjo, L.; Saveant, J. M. J. Electroanal. Chem. Interfacial. Electrochem. 1973, 48, 113.

(31) The relationship is  $k_2' = (Dk_2)^{1/2}$ , where  $D = 1.5 \times 10^{-5}$  cm<sup>2</sup> s<sup>-1</sup> is the diffusion coefficient of Me<sub>2</sub>Co(DpnH).<sup>19</sup> The comparison of the heterogeneous rate process  $(k_{-1})$  with the homogeneous decay  $(k_2)$  as in Scheme I requires the intervention of a third rate process, i.e., mass transport. See ref 17 for additional elaborations of this noint.

17 for additional elaborations of this point.
(32) Bard, A. J.; Faulkner, L. R. "Electrochemical Methods"; Wiley: New York, 1980.

(33) (a) To avoid discontinuity of the discussion at this juncture, the theoretical basis for the evaluation of  $E^{\circ}$  is presented separately in the last part of this paper. (b) The general applicability of this criterion for the determination of the standard electrode potential rests on the independent verification of the kinetics in Scheme I as it applies to Me<sub>2</sub>Co(DpnH).<sup>19</sup>

<sup>(28)</sup> For the significance of these numbers, they should be considered in light of the small reorganization energy  $4\Delta G_0^*$  for Me<sub>2</sub>Co(DpnH). See eq 12-14 and 21.

<sup>(29)</sup> Owing to the constraints of the Nernst equation, Scheme I actually contains only two independent rate constants at any particular value of the applied potential. Thus the general kinetic analysis may be discussed in terms of a two-dimensional diagram and the parameters most conveniently chosen as  $k_2$  and  $k_s$ . (The latter is defined by eq 3.) A detailed analysis of this two-dimensional grid has been performed by Nadjo and Saveant,<sup>30</sup> who identified six kinetic possibilities or zones. We have shown that the steady-state model in eq 8 is generally applicable, by calculations performed in each of these six zones (see the Experimental Section).<sup>18</sup> Saveant's analysis was also extended by treating the sensitivity to the applied potential (i.e.,  $\beta$ ) as an additional or third parameter in the confirmation of the steady-state expression. Thus the validity of eq 8 is not dependent on simplifying assumptions, such as those made in the classical reaction-layer method.



Figure 5. Consistency of the intrinsic barrier  $\Delta G_0^*$  evaluated from the intrinsic rate constant (log  $k_1$ ) by using (a) Marcus eq 12, (b) Rehm-Weller eq 13, and (c) Marcus-Levine-Agmon eq 14 at various potentials.

The curve in Figure 4 encompasses as extensive a span of potentials as possible for a single system. Most importantly, it underscores the important observation of curvature in the relationship between the intrinsic rate constant (log  $k_1$ ) and the applied potential. Since the latter is directly related to the experimental free energy change  $\Delta G$  for electron transfer,<sup>21</sup> the plot in Figure 4 represents an experimental determination of the free energy relationship for electron transfer over an extended region of the free energy change. Our problem now is to determine the functional form of this experimental free energy curve.

Functional Dependence of the Intrinsic Rate Constant  $k_1$  on the Free Energy Change. Experimental Tests of Various Free Energy **Relationships.** The rate constant  $k_1$  for an outer-sphere electron transfer is given in eq 11, where  $\Delta G^*$  is the free energy of activation

$$k_1 = Z \exp(-\Delta G^* / RT) \tag{11}$$

and the collision frequency Z is taken as  $3.5 \times 10^3$  cm s<sup>-1</sup>.<sup>34</sup> Three different relationships are currently in use to relate the activation free energy to the free energy change<sup>21</sup> in electron-transfer reactions.

Marcus<sup>1</sup>

$$\Delta G^* = \Delta G_0^* \left[ 1 + \frac{\Delta G}{4\Delta G_0^*} \right]^2 \tag{12}$$

Rehm-Weller<sup>4</sup>

$$\Delta G^* = \frac{\Delta G}{2} + \left[ \left( \frac{\Delta G}{2} \right)^2 + (\Delta G_0^*)^2 \right]^{1/2}$$
(13)

Marcus-Levine-Agmon<sup>5,35</sup>

$$\Delta G^* = \Delta G + \frac{\Delta G_0^*}{\ln 2} \ln \left[ 1 + \exp\left(-\frac{\Delta G \ln 2}{\Delta G_0^*}\right) \right]$$
(14)

Each of these free energy relationships employs the intrinsic barrier  $\Delta G_0^*$  as the disposable parameter. [The intrinsic barrier represents the activation energy for electron transfer when the driving force is zero, i.e.,  $\Delta G^* = \Delta G_0^*$  at  $\Delta G = 0$  or the equilibrium potential  $E^{\circ}$ .] Since the intrinsic barrier is the single parameter in eq 12, 13, and 14, the applicability of these relationships to the experimental free energy curve in Figure 4 is best carried out by testing each for the consistency of  $\Delta G_0^*$ , which was calculated from the experimental value of  $\Delta G^*$  at each  $\Delta G$ . The result is graphically illustrated in Figure 5. Several features in Figure 5 are noteworthy. First, in the equilibrium region of  $E^{\circ} = 0.53$ V,<sup>33</sup> all three relationships yield a consistent value of the intrinsic barrier as  $\Delta G_0^{\dagger} = 6.3$  kcal mol<sup>-1</sup>. [Note that the scatter of points in the exergonic region arises from the experimental difficulties in the measurement of  $k_e$  (vide supra).] Second, the applicability of the Marcus eq 12 is limited to the region of the free energy change about the equilibrium potential.<sup>36</sup> Significant deviations



Figure 6. Comparison of the experimental rate constant  $k_e$  and the intrinsic rate constant  $k_1$  at various potentials. The ordinate also represents an error expressed in units of kcal mol<sup>-1</sup>.

occur in the endergonic region, particularly at potentials less than  $\sim 0.4$  V. Third, the Rehm-Weller and the Marcus-Levine-Agmon relationships are equally applicable over the entire span of the experimental free energy change. Both relationships yield values of  $\Delta G_0^*$  that deviate less than 0.3 kcal mol<sup>-1</sup> only at the extrema. This test thus represents a unique example of the experimental verification of these free energy relationships over an unusually extended range of the driving force.<sup>37</sup> Owing to its simpler functional form, all subsequent discussions of the free energy relationship for electron transfer will be based on the Rehm-Weller relationship.38

Comparison of the Experimental Rate Constant  $k_e$  and the Intrinsic Rate Constant  $k_1$ . The Discrepancy in the Endergonic Region. The general kinetic expression in eq 10 allows the intrinsic rate constant  $k_1$  to be evaluated from a knowledge of the experimental rate constant  $k_e$  by explicitly taking into account the reversibility in the electron-transfer step according to Scheme I. We must now ask how the magnitudes of  $k_e$  and  $k_1$  differ, particularly over the entire span of the driving force. Unfortunately, the experimental curve for the rate constant  $k_e$  (Figure 3) is not readily distinguished from the curve for the intrinsic rate constant  $k_1$  (Figure 4) by a mere visual comparison. Thus a more descriptive approach to this problem is presented in Figure 6 in which the ratio of the intrinsic and experimental rate constants, i.e., log  $k_1/k_e$ , is plotted against the potential. Two regions of the free energy change can now be readily identified in Figure 6.

(i) For potentials greater than  $\sim 0.4$  V, the experimental rate constant  $k_e$  is indeed an excellent measure of the intrinsic rate constant  $k_1$ . In particular, for the exergonic region beyond 0.53 V, the relationship is given by eq 15. This relationship also Ir

reversible Case: 
$$k_e = k_1$$
 (15)

<sup>(34)</sup> See: Saveant, J. M.; Tessier, D. J. Phys. Chem. 1977, 81, 2192, and ref 18.

<sup>(35)</sup> Levine, R. D. J. Phys. Chem. 1979, 83, 159. Agmon, N.; Levine, R. D. Chem. Phys. Lett. 1977, 52, 197. See also: Scandola, F.; Balzani, V.; Schuster, G. B., in ref 7a.

<sup>(36)</sup> Deviations from the Marcus eq 12 at large driving forces have been noted previously in a variety of homogeneous systems.

<sup>(37)</sup> The Rehm–Weller equation represents a true hyperbolic function of  $\Delta G^*$  and  $\Delta G$ . The Marcus–Levine–Agmon relationship follows a similar functional form but differs slightly at large values of  $|\Delta G|$ . The latter predicts that the rate constant for the anodic process of A will be slightly different than that for the cathodic process of A<sup>+</sup>, when they are evaluated at the same driving force

<sup>(38) (</sup>a) We have also used the Rehm-Weller equation here, since it has been successfully employed to fit the activation energies to an extended region of the driving force in other systems. See: (b) Scandola, F.; Balzani, V. J. Am. Chem. Soc. 1979, 101, 6140 and ref 11-18 cited therein. (c) Kresge, A. J. Chem. Soc. Rev. 1923, 2, 245. (d) Reference 34.



Figure 7. The relationship between transfer coefficient  $\beta_e$  and the error in evaluating the experimental rate constant  $k_e$  as the intrinsic rate constant  $k_1$  for electron transfer according to eq 16.

represents the *irreversible* region of the kinetics since it follows from eq 8 when reverse electron transfer is nil, i.e.,  $k_{-1} \ll k_2'$ .

(ii) For potentials less than  $\sim 0.4$  V, the experimental rate constant  $k_e$  becomes an increasingly inadequate measure of the intrinsic rate constant  $k_1$ . Indeed the discrepancy between these rate constants can be expressed as an error function, i.e.,

$$error = 2.3RT(\log k_1 - \log k_e)$$
(16)

The error thus defines the discrepancy between the experimental rate constant (log  $k_e$ ) and the intrinsic rate constant (log  $k_1$ ) in Scheme I as an energy difference in kcal mol<sup>-1</sup>. We wish to describe how the discrepancy in the endergonic region of Figure 6 arises from the reversibility in the electron-transfer step.

Quantitative Analysis of Reversibility in the Electron-Transfer Step in the Endergonic Region. To understand the origin of the discrepancy between  $k_e$  and  $k_1$  in Figure 6, we note that the error increases as one proceeds further into the endergonic region. Importantly, this trend also coincides with the approach to unit slope in the experimental free energy curve in Figure 3. Therefore, let us now focus on the significance of the slope in the free energy curve.

For heterogeneous electron-transfer processes, reversibility has traditionally been discussed in terms of the magnitude of the experimental transfer coefficient  $\beta_e$ , defined as the tangent to the experimental curve, such as that in Figure 3; i.e.:

$$\beta_{\rm e} = \frac{2.3RT}{n\mathcal{F}} \frac{\partial \log k_{\rm e}}{\partial E}$$
(17)

In particular, the observation of  $\beta_e$  less than unity has been attributed to irreversibility in electron transfer.<sup>39</sup> Accordingly, the potential region above  $\sim 0.4$  V in Figure 3 is consistent with irreversibility since the deviation from the line commences about there. Such an irreversibility based on a value of  $\beta_e$  accords with the conclusion in eq 15. Indeed we have recently extended this type of analysis by showing quantitatively how the experimental transfer coefficient  $\beta_e$  does provide a definitive error limit in the application of eq 15 to any real system.<sup>18</sup> The results of extensive computations show that the error as defined by eq 16 is a smooth function of the magnitude of the transfer coefficient  $\beta_{e}$ , as summarized in Figure 7. (The reader is encouraged to consult the original article, ref 18, for details of the analysis.) It is important to emphasize that the utility of the experimental  $\beta_e$  as an indicator of the error is independent of the magnitude of the intrinsic transfer coefficient  $\beta$ ,<sup>40</sup> which is evaluated at 0.3, 0.5, and 0.7 in Figure 7.



Figure 8. Free energy relationships for electron transfer. Solid heavy curve is the relationship for irreversible electron transfer based on the fit of the Rehm-Weller expression in eq 13. The light lines represent the relationship for reversible electron transfer based on eq 18 with  $k_2' = 1.2$  cm s<sup>-1</sup> (line I) and  $k_2' = 4 \times 10^7$  cm s<sup>-1</sup> (line II) and are drawn with a slope of unity. For the significance of points A, B, C, and D, see text.

Two features in this analysis must be emphasized. First, the energy difference (error limit) between the intrinsic rate constant  $k_1$  and the experimental rate constant  $k_e$  will be less than 0.2 kcal mol<sup>-1</sup> when the experimental transfer coefficient  $\beta_e$  is less than  $\sim 0.7$ . An inspection of Figure 6 confirms this prediction in that such a small error indeed pertains to all the kinetic situations with driving forces greater than 0.4 V.<sup>41</sup> Second, the error limit is seen in Figure 7 to increase catastrophically for values of  $\beta_{e}$  greater than  $\sim 0.7$ , and the experimental rate constant  $k_e$  may no longer be considered as an adequate reflection of  $k_1$ . Consistent with this prediction, the rate constants with values of  $\beta_e$  greater than  $\sim 0.7$  are readily identified as those existing in the potential region below 0.4 V in Figure 3. This situation arises in Scheme I when the rate of back electron transfer is faster than decomposition, i.e.,  $k_{-1} \gg k_2'$ , and eq 8 simplifies to the relationship:  $k_e =$  $k_2'(k_1/k_{-1})$ . We consider this kinetic situation to be the *reversible* limit, since under these conditions the functional dependence of the electron-transfer rate constant on the potential is simply given by the Nernstian expression in eq 18.

Reversible Case: 
$$k_e = k_2' \exp\left[\frac{n\mathcal{F}}{RT}(E - E^\circ)\right]$$
 (18)

To understand better the utility and limitations of  $\beta_e$ , particularly as an error indicator, let us analyze the general kinetics. In particular, we initially considered two limiting kinetic extremes of reversible and irreversible electron transfer, as indicated by the limits of  $k_2'/k_{-1} \ll 1$  and  $k_2'/k_{-1} \gg 1$ , respectively, for the steady-state expression in eq 8. A reversible electron-transfer process, according to eq 18, is one in which the experimental rate constant (log  $k_e$ ) will be a linear function of the potential with a unit slope, since the decomposition rate constant  $k_{2}'$  is independent of the applied potential. This kinetic situation has been plotted in Figure 8 as the light lines I and II at two different, arbitrarily chosen values of  $k_2'$ . An irreversible electron-transfer process according to eq 15 is one in which  $k_e$  will always be equal to  $k_1$ . The anticipated response of the electron-transfer rate constant (log  $k_1$ ) over the extended potential range is indicated by the solid curve in Figure 8, which was drawn on the basis of the Rehm-Weller free energy relationship in eq 13, with  $\Delta G_0^*$  $= 6.3 \text{ kcal mol}^{-1.42,43}$ 

<sup>(39) (</sup>a) The rationale behind this criterion is easily understood with reference to eq 18. According to eq 18, the reversible limit is consistent with only one possible value for  $\beta_e$ , viz., unity. It follows that the further  $\beta_e$  is removed from this benchmark, the higher is the level of confidence with which one can assign the system to the irreversible case. (b) For some relevant examples, see: Saveant, J. M.; Tessier, D. J. Phys. Chem. 1978, 82, 1723. Andrieux, C. P.; Saveant, J. M. J. Electroanal. Chem. Interfacial Electrochem. 1971, 33, 453. Březina, M.; Koryta, J.; Loučka, T.; Maršíková, D.; Pradāč, J. Ibid. 1972, 40, 13. Gileadi, E.; Stoner, G.; Bockris, J. O'M. J. Electrochem. Soc. 1966, 113, 586. Lines, R.; Utley, J. H. P. J. Chem. Soc., Perkin Trans. 2 1977, 804. Louis, C.; Benoit, R. L. Electrochim. Acta 1973, 18, 7.

<sup>(40)</sup> The intrinsic transfer coefficient represents the potential dependence of  $k_1$  in Scheme I.

<sup>(41)</sup> A referee has queried as to how  $k_1$  and  $k_e$  can agree to within 0.2 kcal mol<sup>-1</sup> at 0.45 V when  $k_e$  appears to adhere so closely to the reversible limit between 0.3 and 0.4 V. There is no contradiction, since the transition between reversible and irreversible behavior is expected to be quite rapid ( $\pm$ 50 mV), as described by the discussion of the reversibility factor  $f_r$  in the Experimental Section and Figure 3 in ref 18.

<sup>(42)</sup> At this juncture, we merely employ the Rehm-Weller eq 13 to provide a functional form of the free energy relationship (see Figure 5b). As a completely empirical relationship, it unfortunately provides no insight into the activation process for electron transfer. (For example, see ref 49.)



Figure 9. The intrinsic barrier  $\Delta G_0^*$  evaluated from the experimental rate constant  $k_e$  by using the Rehm-Weller eq 13. Note the deviation of  $\Delta G_0^* = 6.3$  kcal mol<sup>-1</sup> (represented by the horizontal line) in the endergonic region.

Figure 8 thus depicts the possible behavior of the experimental rate constant  $k_e$  in terms of the limiting kinetic situations. Let us now consider the response in the general case. At high values of the driving force, the reverse electron-transfer rate constant  $k_{-1}$  slows down according to eq 3 and approaches zero. Therefore, the extreme exergonic region designated by A in Figure 8 always corresponds to the irreversible limit, i.e.,  $k_{2}' \gg k_{-1}$ . As the value of the applied potential is decreased, the reverse electron-transfer  $k_{-1}$  increases, and one proceeds along the solid curve from the irreversible limit until a point is reached at which  $k_{-1} = k_2'$ . This point occurs at **B** for the one possible value of  $k_{2'}$  depicted by the light line I (with  $k_2' = 1.2 \text{ cm s}^{-1}$ ) in Figure 8. Beyond this point, the system will follow the reversible behavior defined by the line B-D. This simple example underscores two important conclusions. First, large errors in the use of the experimental rate constant  $k_e$ (i.e., point D) for the forward rate constant  $k_1$  (point C) at a given driving force of E' can only occur in the endergonic region where the observed slope  $\beta_e$  is large; i.e., the slope B-D is close to unity. Second, the existence of any error at all (i.e., path A-B-D vs. path A-B-C) is critically dependent on the lifetime of the electrogenerated intermediate  $A^+$ . Thus when  $k_2'$  is sufficiently large (as in the light line II), so that the system always lies in the irreversible region, no error is introduced in equating the experimental rate constant  $k_e$  to the intrinsic rate constant  $k_1$ .

Criterion for Reversibility in the Experimental Rate Constant  $k_e$  and the Determination of  $k_2'$ . Since the interpretation of the experimental rate constant  $k_e$  in the endergonic region depends on the value of the decomposition rate constant  $k_2'$ , we deem it desirable to develop some practical criterion as to whether a reversible or irreversible electron transfer applies at a particular value of the driving force. One possible criterion could be based on a limiting value of the transfer coefficient  $\beta_e = 1$ , as predicted by eq 18 for the reversible limit. However we hasten to add that the observation of a slope of unity in the experimental free energy curve as in Figure 3 is not a sufficient condition for reversibility in the electron-transfer step. Thus consider the Rehm-Weller formulation of the free energy relationship in eq 13, which is rewritten as

$$\Delta G^* (\Delta G^* - \Delta G) = \Delta G_0^{*2} \tag{19}$$

to emphasize its hyperbolic form.<sup>44</sup> The asymptotes of  $\Delta G^* = 0$  and  $\Delta G^* = \Delta G$  predict the transfer coefficients in the exergonic and endergonic limits to be 0 and 1, respectively. The latter ( $\beta = 1$ ) cannot be easily distinguished from the approach to unit slope as a result of the onset of reversibility (i.e., eq 18) in the endergonic region.

A more distinctive approach to this problem involves the measurement of the inherent curvature in the plot of the exper-

Table II. Decomposition Rate Constant  $(k_2)$  Determined from the Wave Shape Analysis of Irreversible Electrochemical CV Data<sup>*a*</sup>

v, V s <sup>-1 b</sup>	<i>E</i> , V <sup>c</sup>	log k <sub>e</sub> , cm s <sup>-1</sup>	$\frac{\log k_1}{\operatorname{cm s}^{-1} d}$	$\frac{\log k_2}{\mathrm{s}^{-1} e},$
0.03	0.318	-3.6800	-3.2254	5.0
0.03	0.347	-3.2700	-2.8962	5.0
0.03	0.373	-2.8900	-2.6105	5.0
0.03	0.399	-2.5600	-2.3341	4.9
0.06	0.358	-3.0600	-2.7743	5.2
0.10	0.368	-2.9300	-2.6648	5.1
0.30	0.346	-3.2100	-2.9074	5.2
0.30	0.383	-2.7200	-2.5031	5.2
0.60	0.361	-2.9100	-2.7413	5.3
1.00	0.377	-2.7900	-2.5674	5.2
3.00	0.368	-2.7800	-2.6648	6.0

<sup>a</sup> In acetonitrile solution containing 0.1 M tetraethylammonium perchlorate at 25 °C. <sup>b</sup> Sweep rate. <sup>c</sup> Applied potential vs. saturated NaCl SCE. <sup>d</sup> Calculated from eq 11 and 13. <sup>e</sup> From eq 20 and the relationship in ref 31.

imental rate constant (log  $k_e$ ) over the entire span of free energy change. Since we have shown in Figure 5 that the curvature can be expressed by a single parameter  $\Delta G_0^*$  in the Rehm-Weller eq 13 for an irreversible charge transfer, the fit of this parameter is a sensitive test for the occurrence of reversibility in the experimental rate constant. Thus with the aid of eq 13, we reevaluated the intrinsic barrier, this time for each measurement of the experimental activation energy  $\Delta G^*$  at the particular driving force. The results of these computations are shown in Figure 9. The fact that the entire region cannot be fitted by any single value of  $\Delta G_0^*$  verifies the composite nature of the experimental rate constant  $k_{e}$ . Thus, in the exergonic region at the high-potential end, there is no notable trend in  $\Delta G_0^*$ , which yields a consistent value of 6.3  $\pm$  0.3 kcal mol<sup>-1</sup>. Since the same value of  $\Delta G_0^*$  was determined in Figures 5b and 5c over the entire span of the free energy change, the consistency provides independent verification of the earlier conclusion in eq 15 that the experimental and intrinsic rate constants coincide in the exergonic region. By contrast, in the endergonic region below  $E^{\circ} = 0.53$  V, there is a clear trend for  $\Delta G_0^*$  to increase with diminishing values of the driving force, in a manner similar to that observed for the error function in Figure 6. Such an increasing discrepancy in  $\Delta G_0^{\dagger}$  is thus clearly associated with the onset of reversibility in the electron-transfer step.

To demonstrate that the method provides a rigorous test for reversibility, we apply the converse argument to show how it can be used to evaluate the decomposition rate constant  $k_2'$  from a knowledge of  $k_e$ . We proceed as follows. First, the rate data in the exergonic region with  $\beta_e < 0.7$  (i.e., path A-B in Figure 8) is used to evaluate  $E^{\circ}$  and  $\Delta G_0^*$  by fitting them to the Rehm-Weller expression. Second, the knowledge of  $E^{\circ}$  and  $\Delta G_0^*$  is sufficient to calculate the intrinsic rate constant  $k_1$  in the endergonic region where  $\beta_e > 0.7$  (i.e., path B-C in Figure 8. Note that this differs from path B-D, which corresponds to the experimental rate constant  $k_e$  in the endergonic region.). Third, the calculated values of  $k_1$ , the experimental values of  $k_e$ , and the standard potential  $E^{\circ}$  (see the next section) are used in conjunction with eq 20 (which is the rearranged form of eq 10) to determine

$$k_{2}' = k_{1}k_{e} \exp\left[-\frac{n\mathcal{F}}{RT}(\mathbf{E}-E^{\circ})\right] / (k_{1}-k_{e}) \qquad (20)$$

the decomposition rate constant  $k_2'$  at various potentials in the endergonic region. The results of the computations are listed in the last column of Table II after conversion to the homogeneous counterpart  $k_2$ .<sup>31,45</sup> It is noteworthy that the value of  $k_2$  deter-

<sup>(43) (</sup>a) The inherent curvature in the plot of the activation free energy in Figure 8 is determined by the parameter  $\Delta G_0^*$ . (b) For a discussion of curvature in free energy relationships, see: ref 2, Balzani, F.; Bolletta, F.; Scandola, F. J. Am. Chem. Soc. **1980**, 102, 2153, and Agmon in ref 7d.

<sup>(44)</sup> For the hyperbolic form of free energy relationships, see a discussion by: Lewis, E. S.; Shen, C. C.; More O'Ferrall, R. A. J. Chem. Soc., Perkin Trans. 2 1981, 1084.

<sup>(45) (</sup>a) For the calculations, values of  $\Delta G_0^* = 6.3 \text{ kcal mol}^{-1}$ ,  $E^\circ = 0.53$  V, and the data in Table I were used. The principal error in this type of analysis is expected to result from locating the potential at which  $\beta_e = \frac{1}{2}$ . Thus an uncertainty of 30 mV in  $E_e^*$  (compare Figure 9) results in an error of one order of magnitude in  $k_2$ . (b) Note that this analysis provides a generally useful method for measuring the decomposition rate constants  $k_2$ ', which would otherwise be very difficult to evaluate.

mined in this manner is in striking agreement with  $k_2 = 10^5 \text{ s}^{-1}$ . which was previously measured by a completely independent kinetic technique.19,46

Determination of  $E^{\circ}$  for Irreversible Electron Transfer. The construction of a free energy curve requires knowledge of the standard potential, which is often difficult to measure in an irreversible process. We wish to show how the curvature in the potential dependence of the experimental rate constant (log  $k_e$ ) can be used to define a unique value of the standard free energy change for outer-sphere electron transfer. In a recent study we established the direct relationship between heterogeneous electrochemical and homogeneous chemical electron transfer in a series of organometal donors.<sup>49</sup> The curvature in the activation free energy relationship was shown to be a property inherent to the electron-transfer process. Indeed the curvature is independent of the experimental means for determining it, whether the method be electrochemical or chemical. This inherent curvature can be used to define a unique value of the experimentally measureable free energy change. In particular, we choose  $\Delta G$  at the observed slope where  $\beta_e$  is equal to 1/2. In other words, from the relationship

$$\Delta G = -n\mathcal{F}(E - E_{\rm e}^{\circ}) \tag{21}$$

 $E_{e}^{\circ}$  is defined to be the potential E at which  $\beta_{e} = 1/2$ . For Me<sub>2</sub>Co(DpnH) in Figure 3 it is 0.53 V.<sup>50</sup>

Having defined  $E_e^{\circ}$  in terms of the experimentally measureable parameters, it is important to address the theoretical significance of this quantity. We begin by noting that the free energy relationship based on the Rehm-Weller expression in eq 13 coincides with that based on the Marcus theory for systems in the region close to the equilibrium potential.<sup>38b</sup> Owing to its theoretical significance, it is advantageous to carry out the further analysis of  $E_e$  in terms of the Marcus theory.<sup>1-3</sup> According to eq 12, the activation free energy  $\Delta G^*$  for outer-sphere electron transfer relates to the standard free energy change  $(\Delta G + w^p)$  through an intrinsic barrier  $\Delta G_0^*$ , where  $w^p$  is the work needed to bring the products together, or bring the product to the electrode.<sup>51</sup> (For neutral reactants such as  $Me_2Co(DpnH)$ , we consider the work term  $w^r$ to be nil.<sup>52</sup>) The Marcus theory predicts a quadratic dependence of the activation free energy  $\Delta G^{\dagger}$  on the thermodynamic driving force. Notably eq 12 predicts a slope of 1/2 at  $(\Delta G + w^p) = 0$ , and this prediction has been verified in numerous examples.<sup>15,53</sup> Although the experimental dependence in Figure 4 is more complicated than the simple parabolic shape predicted by eq 12, the point at which  $\beta_e$  is equal to 1/2 is unique. Therefore if the Marcus theory applied to Me<sub>2</sub>Co(DpnH), the experimentally measureable

 (47) Nicholson, R. S.; Shain, I. Anal. Chem. 1964, 36, 706.
 (48) MacDonald, D. D. "Transient Techniques in Electrochemistry"; (49) MacDonald, D. D. Tansient Techniques in Electrochemistry ,
 (49) Klingler, R. J., Kochi, J. K. J. Am. Chem. Soc. 1981, 103, 5839.

(50) The values of  $E_e$  can also be extracted from routine CV data of irreversible systems by the straightforward procedures described in the Experimental Section. The procedure is mathematically equivalent to drawing chords between data points of log  $k_e$  in Figure 3 and plotting the resultant slopes against the applied potential. A value of  $E_e^* = 0.52$  V is obtained in Figure 10 in the Experimental Section.

(51) For the discussion of the work terms, see the discussion by: Mohilner, D. M. J. Phys. Chem. 1969, 73, 2652. Note that in eq 12, w<sup>p</sup> was not included in the free energy change. See ref 54.

parameter  $E_{e}^{\circ}$  must have the value given by eq 22, where  $w^{p'} =$ 

$$E_{\rm e}^{\circ} = E^{\circ} + (n\mathcal{F})^{-1}[w^{\rm p} + 4w^{\rm p'}\Delta G_0^{*}/(1+w^{\rm p'})] \qquad (22)$$

 $\partial w^p / \partial \Delta G$ . Equation 22 predicts that  $E_e^*$  will only differ from the standard reduction potential E° by the function of the work term in the brackets. Provided there is no specific interaction with the electrode surface, the outer-sphere work terms are expected to be small and may be approximated by appropriate electrostatic models.54 The question of the specific interaction with the electrode has been resolved in this organometal system since the direct correspondence of the electrochemical and chemical rate constants has demonstrated a common outer-sphere mechanism for these oxidations.49

#### Summary and Conclusion

The experimental rate constants  $k_e$  for outer-sphere electron transfer in Figure 3 span the extended range of free energy changes from the exergonic to the endergonic limits. With regard to the generalized kinetic Scheme I, the exergonic region is characterized by (i) the experimental rate constant  $k_e$ , which approaches the intrinsic rate constant  $k_1$ , (ii) the transfer coefficient, which approaches a limiting value  $\beta_e = 0$ , and (iii) the rate constant  $k_2'$  $\gg k_{-1}$ , which also makes it the irreversible kinetic limit. The endergonic limit is characterized by (a) the experimental rate constant  $k_{\rm e}$ , which approaches  $k_2'(k_1/k_{-1})$ , (b) the transfer coefficient, which reaches a limiting value of  $\beta_e = 1$ , and (c) the rate constant  $k_{-1} \gg k_2'$ , which also makes it the reversible kinetic limit.

The transfer coefficient  $\beta_e$  uniquely defines the irreversible limit in the exergonic region; i.e.,  $\beta \rightarrow 0$  is concurrent with  $k_{-1}/k_{2}' \rightarrow 0$ 0. In particular, those portions of the experimental free energy curve that exhibit  $\beta_e$  less than 0.7 may be assigned to the irreversible kinetic limit for electron transfer (i.e., eq 15). They yield experimental rate constants (log  $k_e$ ) that agree with the intrinsic rate constant (log  $k_1$ ) to within 0.2 kcal mol<sup>-1</sup> (Figure 6).

The utility of  $\beta_e$  as a measure of the irreversibility in the electron-transfer step diminishes as it approaches 1 in the endergonic region, as indicated by the error limits in Figure 7. Indeed the limiting value of  $\beta = 1$  is equally consistent with either reversible or irreversible electron transfer, as illustrated in Figure 8. Fortunately with Me<sub>2</sub>Co(DpnH), the availability of an independent determination of the decomposition rate constant  $k_2$ provides the necessary information to analyze the kinetics in the endergonic region. Thus the intrinsic rate constant  $k_1$  can be expressed analytically as a function of the experimental rate constant  $k_e$  by explicitly taking into account reversibility according to eq 10. The intrinsic rate constant (log  $k_1$ ) obtained in this manner is shown in Figure 5 to fit the Rehm-Weller and Marcus-Levine-Agmon free energy relationships over the entire span of the driving force with a single value of the intrinsic barrier,  $\Delta G_0^* = 6.3$  kcal mol<sup>-1</sup>. Thus the experimental transfer coefficient  $\beta_e$  in the endergonic region reflects both electron-transfer reversibility as well as the potential dependence of the intrinsic rate constant (log  $k_1$ ), the relative importance of each depending on the value of  $k_2'$ .<sup>55</sup> By utilizing this interdependence, a method is outlined that analyzes the experimental free energy curve to allow the decomposition rate constant  $k_2'$  to be evaluated in Table II.

<sup>(46)</sup> Such a lifetime is generally determined for systems in which both the anodic and cathodic CV waves can be observed by a standard analysis of the sweep rate of the current-potential function.<sup>47,48</sup> However, for systems such as Me<sub>2</sub>Co(DpnH), which exhibit irreversible CV waves of the type shown in Figure 1, this type of analysis is impossible. Fortunately, this problem may be resolved by the appropriate combination of chemical and electrochemical techniques. For example, the electrolysis of Me<sub>2</sub>Co(DpnH) at constant current provides a well-defined flux of methyl radicals whose kinetics may be examined by the competition method with suitable chemical trapping methods. See ref 19 for details.

<sup>(52) (</sup>a) The work term of the reactants is omitted in eq 12, since it is taken as zero for the neutral reactants such as Me<sub>2</sub>Co(DpnH), as described in ref 19. (b) See ref 14 and 34.

<sup>(53) (</sup>a) The slope is actually  $\frac{1}{2} + w^{p}$ , but  $w^{p} \sim 0$  (see ref 34). (b) For leading references, see: Sutin, N. In "Inorganic Biochemistry"; Eichhorn, G. L., Ed.; Elsevier: Amsterdam, 1973; Vol. II, p 611 ff, and ref 8 and 15. Hale, J. M. In "Reactions of Molecules at Electrodes"; Hush, N. W., Ed.; Wiley: New York, 1971, p 229.

<sup>(54) (</sup>a) Since both work terms are small for these systems (see ref 49), we have employed  $E_e^{\circ}$  as equal to  $E^{\circ}$  throughout this study. The assumption that the work terms in this system are small is strongly supported by the direct comparison of the heterogeneous electrochemical rate data with the homogeneous chemical rate data, as described in ref 13b, 19, and 49. (b) Calculations based on a dielectric continuum model have been typically for electron transfer in homogeneous systems. (See Marcus in ref 1 and Brown, G. M.; Sutin, N. J. Am. Chem. Soc. 1979, 101, 883.) In heterogeneous electrochemical systems, the dielectric continuum model of Gouy-Chapman (as modified by Stern for the finite size of the ionic radius of the supporting electrolyte) has been often used. See ref 9b and 10b.

<sup>(55)</sup> For example, the error function arising from electron-transfer reversibility in Figure 6 is  $\sim 1 \text{ kcal mol}^{-1}$  at 0.3 V for Me<sub>2</sub>Co(DpnH). Thus most of the slope in Figure 3 at this potential arises from the potential dependence of the intrinsic rate constant shown in Figure 4.

Table III. Measurement of the Uncompensated Cell Resistance<sup>a</sup>

ω, Hz	<i>i</i> , µA	Ζ, Ω	
1	1.15	83000	
10	7.2	14000	
100	50	2000	
1000	370	270	
10000	2500	34	

<sup>a</sup> See text for definitions.

The experimental free energy relationship includes the point where E = 0.53 V, at which the transfer coefficient  $\beta_e$  is equal to 1/2. To interpret the theoretical significance of  $\Delta G$ , we turn to the Marcus theory, which states that  $\Delta G = -n\mathcal{F}(E - E_e^\circ)$ , where  $E_e^\circ$  is the standard reduction potential  $E^\circ$  plus the work terms, which are small for the outer-sphere process examined in this study. Thus at  $\beta_e = 1/2$ , E is defined to be  $E_e^\circ$  and  $\Delta G = 0$ . The intrinsic barrier  $\Delta G_0^*$  can be evaluated at this point, or more equitably by the use of the kinetic data (log  $k_1$ ) over the entire free energy span by using the free energy relationships, as in Figure 5. The cyclic voltammetric determination of the transfer coefficient at  $\beta_e = 1/2$  also provides a convenient method to evaluate the standard reduction potentials for irreversible systems (see Figure 10 in the Experimental Section).

#### **Experimental Section**

**Materials.** The preparation of  $Me_2Co(DpnH)$  was described previously.<sup>19</sup> Reagent grade acetonitrile (Fisher Chemical Co.) was further purified by refluxing it over calcium hydride, then treated with potassium permanganate, and redistilled from  $P_2O_5$  through a 19-plate bubble cap Oldershaw column. Tetraethylammonium perchlorate (TEAP) was obtained from the G. F. Smith Chemical Co. and dried in vacuo at 60 °C.

Electrochemical Measurements. Electrochemistry was performed on a Princeton Applied Research Model 173 potentiostat equipped with a Model 176 current-to-voltage converter that provided a feedback compensation for ohmic drop between the working and reference electrodes. The high impedance voltage follower amplifier (PAR Model 178) was mounted external to the main potentiostat to minimize the length of the connection to the reference electrode. This arrangement ensured low noise pickup. Cyclic voltammograms were recorded on a Houston Series 2000 X-Y recorder. The electrochemical cell was constructed according to the design of Van Duyne and Reilley.<sup>56</sup> The distance between the platinum working electrode and the tip of the salt bridge was 1 mm to minimize ohmic drop. The performance of the electrochemical systems was initially tested by applying a 100-mV peak-to-peak sinusoidal wave and measuring the resultant ac current with a PAR Model 5203 lock-in amplifier. The current i measured at various frequencies  $\omega$  is listed in Table III. Extrapolation of the observed impedance Z to infinite frequency (i.e.,  $\omega^{-1}$  extrapolated to zero) establishes an upper limit of 2 ohms for the uncompensated cell resistance. Digital current-time data for the convolution linear sweep voltammetry were recorded on a Princeton Applied Research Model 4102 transient signal recorder. The signal recorder was interfaced to a Digital Equipment Corp. PDP 11/23 computer. All computations were performed on this system.

Convolutive Potential Sweep Voltammetry. All electrochemical measurements were carried out at 25 °C in acetonitrile solutions, with 0.26 M tetraethylammonium perchlorate as supporting electrolyte. The platinum electrode was initially cleaned by soaking it in concentrated nitric acid for 1 h, followed by repeated rinsing with distilled water and drying at 120 °C prior to use. In between each scan, the electrode was cleaned with a fine polishing cloth, as described below. In addition, the cracked-tip salt bridge was stored in a solution of acetonitrile that was 0.26 M in TEAP when not in use. Under these conditions the day-to-day reproducibility of the peak potential measurements at 100 mV s<sup>-1</sup> was  $\pm 10$  mV.

During a typical experiment, the electrochemical cell was filled with a solution of acetonitrile containing only 0.26 M TEAP. The applied potential was alternately stepped to -2.0 V vs. SCE for 5 s and then returned to 0.0 V sequentially 3 times in succession. The latter procedure was found to improve the reproducibility of the background charging current. The charging current was recorded at least twice, and checked to be reproducible to within  $\pm 5\%$  by a comparative procedure utilizing the two memories of the transient signal recorder. The dwell time for sampling the current was optimized between 50 ms and 25  $\mu$ s to obtain up to 1000 data points per sweep. The solution was gently drained Klingler and Kochi

through the bottom of the cell and replaced with a  $2.12 \times 10^{-3}$  M solution of Me<sub>2</sub>Co(DpnH) in acetonitrile (0.26 M in TEAP). The current data were recorded again at least twice, and checked to be reproducible to within  $\pm 5\%$ . In between runs, the cell was cleaned with an acetonitrile solution containing 0.26 M in TEAP, and the electrode was buffed with a fine polishing cloth.

The convolution integral,  $\Psi(t)$  in eq 23, is related to the time-de-

$$\Psi(t) = \frac{10^3}{n\mathcal{F}AC^0(\pi D)^{1/2}} \int_0^t i(\eta)(t-\eta)^{-1/2} \,\mathrm{d}\eta \tag{23}$$

pendent concentration in eq 7:

$$C(t) = C^{0}[1 - \Psi(t)]$$
(24)

The convolution integral,  $\Psi(t)$ , was evaluated by conversion to the finite summation in eq 25, where  $\theta$  is the dwell-time interval between the data

$$\Psi(t) = (\theta/\pi)^{1/2} \sum_{n=0}^{m} a_{n+1} i_{m-n}$$
(25)

points, and m is the number of subintervals within the time period t defined according to  $m = t/\theta$ . The current  $i_{m-n}$  is evaluated at the time  $\theta(m-n)$ , and the coefficients  $a_n$  are obtained according to the relationship

$$a_n = (4n\sqrt{n} + (8 - 8n)\sqrt{n - 1} + (4n - 8)\sqrt{n - 2})/3 \quad (26)$$

which only applies for n > 1 (note:  $a_1 = \frac{4}{3}$ ). Integration with the coefficients defined by eq 26 is exact if the current can be considered to be a linear function of the time within the subintervals of length  $\theta$ . This will always be true for a sufficiently short time interval. In practice, the values obtained from eq 26 were found to be rather insensitive to the coarseness of the time grid  $\theta$ , provided the wave was divided into at least 20 intervals. The resultant convolution integral-time data were converted into the corresponding convolution integral-potential set by noting that  $E = E_1 + vt$ , where  $E_1$  and v are the initial potential and the sweep rate, respectively. Finally, the area of the electrode was determined from the limiting value  $\Psi_L$  of the convolution integral, in which case eq 6 (see Results) reduces to

$$k_{\rm e}(E) = D^{1/2} i(E) / (\Psi_{\rm L} - \Psi_{E})$$
<sup>(27)</sup>

as discussed by Imbeaux and Saveant.<sup>27</sup> The FORTRAN program for evaluating eq 25-27 was tested with the theoretical current-potential data tabulated by Nicholson and Shain<sup>47</sup> for a totally irreversible CV wave, and it is available upon request.

Determination of  $E_e^*$  for the Log  $k_e$  Data. Examination of Figure 3 indicates that the experimental slope varies smoothly from 0.9 to 0.3. However, despite the determination of over 1500 rate constant data, there is still sizeable scatter in the result. This scatter will be greatly magnified by any numerical differentiation process. The analysis of Figure 5 indicates that the two-parameter Rehm-Weller equation empirically fits the data for values of the applied potential greater than 0.44 V. Therefore, this equation was used to determine the point at which the slope is 0.5 by the following procedure: First, an  $E_e^*$  value of 0.55 V was graphically estimated and used to calculate a set of  $\Delta G_0^*$  values as described in the text. These  $\Delta G_0^*$  values were averaged and used to calculate the point at which the slope was 1/2. The calculations carried out by this procedure provided a better estimate of  $E_e^*$  from the rate constant data. This process was repeated until a consistent pair of  $E_e^* = 0.53 \pm 0.01$  and  $\Delta G_0^* = 6.3 \pm 0.05$  were obtained for Figure 3.

**Determination of E\_c from Current-Potential Data.** As discussed previously,<sup>18</sup> the location of the current peak in the CV experiment for a totally irreversible system corresponds to a measurement of the electron-transfer rate constant  $k_e$  according to<sup>57</sup>

$$k_{\rm e} \,({\rm at} \,E_{\rm p}) = 2.18 (D\beta n \mathcal{F} v/RT)^{1/2}$$
 (28)

where v is the sweep rate. An analogous equation exists for the half-peak potential  $E_{p/2}$ .<sup>58</sup>

$$k_{\rm e} ({\rm at} \ E_{\rm p/2}) = 0.34 (D\beta n \mathcal{F} v / RT)^{1/2}$$
 (29)

Consideration of eq 28 and 29 indicates that the experimental location

ip.

<sup>(57)</sup> This conclusion is not completely unexpected, since the CV method summarized by eq 28 can be derived from eq 6. Thus Nicholson and Shain<sup>47</sup> have shown for linear sweep voltammetry that the current peak  $i_p$  will occur when the concentration C(t) has dropped to 22.7% of  $C^0$ . Proceeding from eq 6, it then follows that  $k_e(E_p) = (n\mathcal{FA})^{-1}i_p/0.227C^0$ , which is identical with eq 28 since the peak current is given by<sup>47</sup>  $i_p = 0.4958 n\mathcal{FA}C^0(Dn\mathcal{Fv}/RT)^{1/2}$ . (58) Defined as that potential at which the current is 1/2 the peak current

<sup>(56)</sup> Van Duyne, R. P.; Reilley, C. N. Anal. Chem. 1972, 44, 142.



Figure 10. The dependence of the experimental transfer coefficient  $\beta_e$  on the applied electrode potential *E* for Me<sub>2</sub>Co(DpnH) in CH<sub>3</sub>CN containing 0.26 M TEAP at 25 °C.

of the peak potential  $E_p$  and the half-peak potential  $E_{p/2}$  corresponds to the determination of a chord between two points in the rate data shown in Figure 3. Simple rearrangement of eq 28 and 29 yields the result originally given by Nicholson and Shain,<sup>47</sup> i.e.:<sup>59</sup>

$$\beta_{\rm e} = \frac{1.857RT}{n\mathcal{F}} (E_{\rm p} - E_{\rm p/2})^{-1} \tag{30}$$

The values of  $\beta_e$  thus obtained are plotted against the average of  $(E_p + E_{p/2})/2$  in Figure 10. The value at which the observed transfer coefficient  $\beta_e$  equals  $1/_2$ , viz.,  $E_e^* = 0.52 \pm 0.01$ , is readily obtained by this procedure and compares quite favorably with that obtained from analysis of the rate constant data in Figure 3.

Reversibility Factor  $f_r$  and Electrochemical Kinetics of Scheme III. The electrochemical problem in cyclic voltammetry is readily described on the basis of the simple kinetic Scheme III, which is a more detailed electrochemical form of Scheme I, where the subscripts 0 and s refer to

#### Scheme III

$$A_0 \frac{k_1}{k_1} A_0^+$$
(31)

$$A_0^+ \xrightarrow{k_d} A_s^+ \tag{32}$$

$$A_0^+ \xrightarrow{\kappa_r} B_s$$
 (33)

the concentrations at the electrode surface and in the bulk solution, respectively. In the usual situation, the electrochemical current corresponds to the difference between the rate of the forward electron transfer and that of the reverse step, as given in eq 34. The concentration of the

$$i/n\mathcal{F}A = k_1[A_0] - k_{-1}[A_0^+] \tag{34}$$

intermediate  $[A_0^+]$  is given in terms of the rate constants in Scheme III as

$$[A_0^+] = [A_0]k_1/(k_{-1} + k_2')$$
(35)

where  $k_2' = k_r + k_d$ .<sup>60</sup> The validity of eq 35 (which is tantamount to a steady-state kinetic analysis) has been verified by the rigorous solution of the inhomogeneous kinetics described in Scheme III.<sup>29</sup> The combination of eq 6 with eq 34 and 35 yields the expression for the net forward rate constant in terms of the fundamental kinetic parameters in Scheme III as

$$k_{\rm e} = k_1 k_2' / (k_{-1} + k_2') \tag{36}$$

In the CV experiment, total irreversibility can be achieved by (1) enhancing the chemical reactivity of the electrogenerated intermediate  $A_0^+$  (i.e., increasing  $k_r$  in eq 33) and/or (2) increasing the rate of mass transport of  $A_0^+$  from the electrode surface by the variation in the sweep rate (i.e.,  $k_d$  in eq 32).<sup>17</sup>

Electrochemical reversibility in cyclic voltammetry has been discussed in terms of the reversibility factor  $f_r$  in eq 37 as that fraction by which

(59) This analysis assumes the transfer coefficient to be effectively a constant over the width of the CV wave, an operation that is similar to drawing chords between individual data points in Figure 3.



Figure 11. Variation of the reversibility factor  $f_r$  as a function of the rate constant ratio  $k_{-1}/k_2'$ .

the concentration ratio of the electroactive species ( $A_0$  and  $A_0^+$  in Scheme III) has been reduced from the value predicted by the Nernst equation, i.e.,<sup>18</sup>

$$\frac{[A_0^+]}{[A_0]} = f_r \exp\left[\frac{n\mathcal{F}}{RT}(E - E^\circ)\right]$$
(37)

Defined as such,  $f_r$  varies smoothly between the limits of unity and zero for the limiting kinetic situations described above as reversible and totally irreversible, respectively. The reversibility factor  $f_r$  is directly related to the intrinsic kinetic parameters in Scheme III according to eq 38. Figure

$$\frac{f_{\rm r}}{1-f_{\rm r}} = \frac{k_{-1}}{k_2'} \tag{38}$$

11 illustrates how the reversibility factor is a smooth function of the rate constant ratio  $k_{-1}/k_2$ .

Let us now consider how the magnitude of the reversibility factor defines the reversible and irreversible limits of electron transfer for the kinetics in Scheme III.

A. Reversible Electron Transfer. As the reversibility factor  $f_r$  approaches unity, the observed rate constant for net electron transfer will approach the functional form given by eq 39, which derives from a consideration of eq 36 and 38, with  $k_{-1} \gg k_2$ '.

$$k_{\mathbf{e}} = k_{2}' \exp\left[\frac{n\mathcal{F}}{RT}(E - E^{\mathbf{e}})\right]$$
(39)

Since  $k_2'$  is independent of the applied potential, eq 39 predicts the observed rate constant (log  $k_e$ ) to be a linear function of *E* with a slope of unity. Inspection of the experimental results in Figure 3 indicates such a prediction is borne out only in the highly endergonic region—the deviation from a unit slope is increasing, especially at the larger values of the applied potential. Thus the oxidation of Me<sub>2</sub>Co(DpnH) does not conform to a reversible Nernstian couple over the potential range of 0.3–0.8 V vs. SCE in Figure 3. It is just this deviation from reversible behavior that allows the determination of the intrinsic rate constant  $k_1$  for heterogeneous electron transfer.

**B.** Irreversible Electron Transfer. As the reversibility factor  $f_r$  approaches zero, the observed rate constant for net electron transfer will become equal to the forward rate constant  $k_1$ , which derives from a consideration of eq 36 and 38, with  $k_2' \gg k_{-1}$ . In this limit, the slope of the free energy relationship in Figure 3 represents the electrochemical transfer coefficient  $\beta$ , i.e.,

$$\beta_{e} = \frac{2.3RT}{n\mathcal{F}} \left( \frac{\partial \log k_{e}}{\partial E} \right) = \frac{2.3RT}{n\mathcal{F}} \left( \frac{\partial \log k_{1}}{\partial E} \right) = \beta \qquad (40)$$

The measured value of the transfer coefficient  $\beta_e$  and the true  $\beta$  for the intrinsic rate constant coincide at this irreversible limit.

C. Comparison of the Rate Constants  $k_2$ ' and  $k_{-1}$ . An important feature in Figure 11 is the rapid transition between reversible and irreversible behavior that occurs in the region centered about the point at which  $k_2$ ' =  $k_{-1}$ . Thus the variation of only 0.43 in log  $(k_{-1}/k_2')$  corresponds to a decrease of the reversibility factor  $f_r = 0.75$  to 0.25. Systems that exhibit  $f_r < 0.25$  may be assigned to the irreversible case (eq 15) with a confidence level of 0.2 kcal mol<sup>-1,18</sup> On the basis of eq 3, the variation of log  $(k_{-1}/k_2') = 0.43$  is expected to occur within a potential region of 50 mV, assuming an average transfer coefficient  $\beta$  of 0.5 for the general case. In the Me<sub>2</sub>Co(DpnH) system,  $k_2'$  has been evaluated as 1.2 cm s<sup>-1</sup>.<sup>19</sup> While  $k_{-1}$  is not directly measured, it may be calculated from the values of  $k_1$  listed in Table I and the Nernst equation with  $E^{\circ} = 0.53$ V to have the value of 1.2 cm s<sup>-1</sup> at E = 0.36 V. Thus the transition in the reversibility factor from  $f_r = 0.75$  to 0.25 is expected to occur in Figure 9 over a rather limited region of the applied potential between 0.31 and 0.41 V. This is graphically demonstrated by the marked curvature

<sup>(60)</sup> The appropriate conversion of the heterogeneous rate constant  $k_r$  to the homogeneous chemical rate constant  $\kappa$  is given by  $k_r = (D\kappa)^{1/2}$ , and the transport rate constant  $k_d$  (in cm s<sup>-1</sup>) due to planar diffusion in linear sweep voltammetry is given by  $k_d = 2.82 (nDv)^{1/2}$  where D is in units of cm<sup>2</sup> s<sup>-1</sup> and v in V s<sup>-1</sup>. See ref 31.

of the plot in the potential region below 0.4 V in Figure 9, which is notably absent in the plot derived from the complete kinetic situation presented in Figure 5a.

Peak Broadening of the CV Wave and the Nature of the Electrochemical Reversibility. In the kinetics of Scheme III, the disappearance of the electrogenerated intermediate  $A_0^+$  depends on the overall rate constant  $k_2'$ . Actually, two pathways exist for the depletion of  $A_0^+$ , viz., the diffusion rate constant  $k_d$  in eq 32 and the chemical reaction rate constant  $k_r$  in eq 33.

Diffusion is known to be proportional to the square root of the sweep rate,<sup>24</sup> whereas  $k_r$  will be a constant that is specific to the chemical system, i.e., the chemical identity of  $A_0^+$ . Both processes operate simultaneously in the inhomogeneous concentration profile extant at the electrode surface. Nonetheless, it has been shown that the net effect  $k_2'$  may be described as a simple sum of the two rate processes, i.e.,<sup>18,60</sup>

$$k_{2}' = k_{\rm r} + k_{\rm d}$$
 (41)

The results in Figure 2 indicate that the net forward rate constant  $k_e$ in eq 36 is independent of the sweep rate varying over 4 orders of magnitude. This is consistent with the generation of a highly unstable intermediate in which  $k_2$ ' is dominated by  $k_r$  over the entire range of accessible sweep rates.<sup>61</sup> This result has important implications. Thus, the CV waves in Figure 1 are observed to broaden (as measured by  $E_p$  $-E_{p/2}$ ) substantially at higher sweep rates. This broadening is not due to a decrease in the electrochemical reversibility.<sup>62</sup> For example, if  $k_2'$ were controlled by  $k_d$ , the maximum slope of the plot of log k vs. log v would be 0.5 for systems in which electrochemical reversibility (as defined by eq 37 and 38) is determined by the sweep rate.

Furthermore, we can conclude that the broadening of the CV waves in Figure 1 is not due to an experimental artifact such as an uncompensated cell resistance.<sup>63</sup> Thus at any constant value of the applied potential, the current increases as the square root of the sweep rate. Yet the value of the measured rate constant is invariant, as shown by the horizontal rows in Figure 2. Therefore, uncompensated iR drops have a minimal influence on the rate data. Indeed, the slopes in Figure 2 in conjunction with eq 42 may be used to estimate an upper limit on the uncompensated cell resistance,

$$d \log k_{e} = (\beta n \mathcal{F} / 2) V_{cell} d \log v$$
(42)

where  $V_{cell} = iR_{cell}$ . Since the slopes in Figure 2 are all close to zero, the uncompensated cell resistance must also be close to zero, according to eq 42. Indeed, this conclusion accords well with the results obtained from Table III.

We can thus conclude that the broadening of the CV waves with sweep rate is not due to (1) changes in degree of electrochemical reversibility or (2) experimental artifacts such as uncompensated cell resistance. However, such a peak broadening could result directly if the transfer coefficient  $\beta_e$  were itself a function of the applied potential. Thus standard electrochemical theory indicates that the width of the CV wave will be given by eq 30. Indeed the plot of  $k_e$  vs. E in Figure 3 indicates a substantial degree of curvature, consistent with a potential dependence of  $\beta$ .49

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Supplementary Material Available: Tabulation of the experimental rate constants  $k_e$  and electrochemical data used (27 pages). Ordering information is included on any current masthead page.

## Micellar Photochemistry. Photooxidations with Intramicellar-Generated Singlet Oxygen

## Michael C. Hovey

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Abstract: Pyrex-filtered irradiation of an aerated 5% aqueous sodium dodecyl sulfate (NaDodSO<sub>4</sub>) solution of 2.8 mM 10-methylphenothiazine (MPT) and 2.8 mM benzyl sulfide resulted in formation of a 39% yield of benzyl sulfoxide. The reaction was general for transformation of a variety of sulfides to sulfoxides and for triphenylphosphine to triphenylphosphine oxide and was catalytic with respect to MPT. Also effective in promoting the photooxidation were 10-acetylphenothiazine, 10-benzoylphenothiazine, 10-(2-cyanoethyl)phenothiazine, 10-methyl-2-(trifluoromethyl)phenothiazine, and 3-bromo-10methylphenothiazine. The photooxidation also took place in microemulsion media. Singlet oxygen was implicated as the primary oxidizing agent and is thought to arise by the intramicellar recombination of the transient  $MPT^+/O_2^-$  ion pair. The rates of quenching of  ${}^{1}O_{2}$  by benzyl sulfide and MPT were measured in chloroform solution. The quenching rate,  $k_{Q}$ , was 6.4 × 10<sup>6</sup> M<sup>-1</sup> s<sup>-1</sup> for benzyl sulfide and 2.9 × 10<sup>6</sup> M<sup>-1</sup> s<sup>-1</sup> for MPT. The reaction of singlet oxygen with benzyl sulfide in the presence of MPT in the micelle was discussed in terms of the greater tendency of the MPT to quench singlet oxygen rather than react to form 10-methylphenothiazine 5-oxide.

Aqueous micellar medium effects on photophysical processes have seen much attention recently.<sup>1</sup> The use of micelles to promote synthetically useful photochemical reactions is an area of rapidly increasing interest. Some examples of synthetic reactions include photocycloadditions,<sup>2</sup> substitutions,<sup>3</sup> isotopic en-

richment,<sup>4</sup> and remote functionalization.<sup>5</sup> In contrast to those in homogeneous solution, products and yields often change dra-

<sup>(61)</sup> In other words, the electrochemical irreversibility induced by the fast following chemical reaction is already so large that the reversibility of the system cannot be significantly altered, even by employing sweep rates as high as 1000 V s<sup>-1</sup>

<sup>(62)</sup> The interpretation of the broadening and concurrent shifting of the CV wave as due to changes in the electrochemical reversibility of the system while a constant value of the transfer coefficient is maintained is the basis of the method proposed by Nicholson<sup>63</sup> for obtaining the data for heterogeneous rate constants.

<sup>(63)</sup> The broadening effect of CV waves arising from uncompensated cell resistance is known. See: Nicholson, R. S. Anal. Chem. 1965, 37, 1351.

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